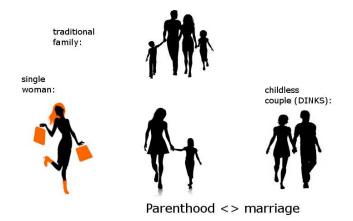
DINKS, DEWKS & Co. Marriage, Fertility and Childlessness in the US

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Various family types



Q: Which single women become mothers and which married women remain childless?

 Introduction
 Stylized facts
 Theory
 Regimes
 Identification
 Comparative Statics
 conclusion
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Answers from the literature

Dynamic models of marriage (and divorce) with endogenous fertility:

- Greenwood, Guner & Knowles (2003) (expl. decline of marriage and rise of divorce)
- Regalia, Ríos-Rull & Short (2008) (expl. increase in singleness)

On childlessness:

- Social sciences distinguish Involuntary vs Voluntary childlessness (Poston & Trent (1982), Morgan (1991), Toulemon (1996))
- Economics: Gobbi (2011) childlessness rate and fertility rate not necessarily negatively correlated over time at macro level

Our contribution

A theory to explain jointly marriage/singleness and parenthood/childlessness decisions.

Co-existence of involuntary and voluntary causes of childlessness is key to explain facts (US, 1990)

- 5.8% of American women are involuntarily childless
- 9% are voluntarily childless

Predictions: How better education of women and men affect both types of childlessness and fertility.

US Census data

Data: US Census, 45-70 year old married and never married women in 1990. Completed fertility

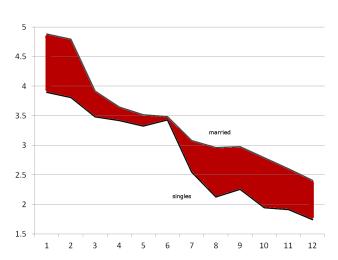
Drop Separated, Widowed and Divorced ($\approx 30\%$), concentrate on Married and Single

Potential income - 12 education categories - 1127080 obs

Nb	Category	N. obs.	Nb	Category	N. obs.
1	No school	12122	7	Grade 12	479703
2	Grade 1-4	14050	8	1 year of college	178274
3	Grade 5-8	84243	9	2 years of college	53428
4	Grade 9	38121	10	Bachelor degree	99046
5	Grade 10	57213	11	Master degree	56855
6	Grade 11	49413	12	Doctoral degree	4612

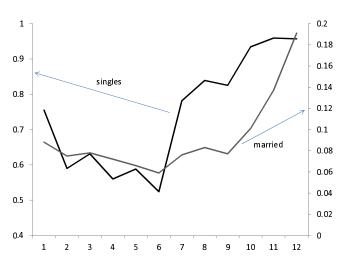
Fact 1: fertility gap

When mothers, singles' fertility is lower by no more than one child compared to married



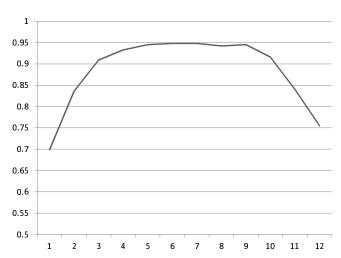
Fact 2: childlessness

Childlessness exhibits an U-Shaped relationship with education for both singles and married



Fact 3: marriage

There is a hump-shaped relationship between marriage rates and education levels



Main features of the model

Static model, 2 sexes $(i = \{f, m\})$, agents decide

- to marry or not (random matching, once in life)
- Consumption and fertility

Women can have children, married or not \neq Men should marry to have children

Exogenous potential income (education): wi

+ heterogeneity in non labor income $a^i \perp w^i$

Preferences

Individuals:

$$u\left(c^{i},n\right)=\ln c^{i}+\ln \left(n+\nu\right)$$

No gender differences in preferences $\nu >$ 0: Services from children are superior good

Couples:

$$\theta \ u(c^f, n) + (1 - \theta) \ u(c^m, n)$$

with

$$\theta \equiv \frac{1}{2} \, \underline{\theta} + (1 - \underline{\theta}) \frac{w^f}{w^f + w^m}, \qquad \underline{\theta} \in (0, 1)$$

 \Rightarrow although \exists marriage surplus, one spouse may refuse marriage if she/he is too low educated relatively (low θ / $1-\theta$)

Marriage

Random matching, once in life

Gain to be married for a man: having children, potentially increasing consumption, household public good

Gain to be married for a woman: sharing childrearing costs, potentially increasing consumption, household public good

Cooperative bargaining: there is always a marriage surplus, but if power is too unequally distributed, better to stay single

Minimal consumption to be able to procreate: c^{min}

$$n > 0 \Rightarrow c^f \ge c^{\min}$$

Why? Mc Fall, (1979): Poor are more subject to diseases that can lead to subfecundity

- Malnutrition
- Poor use more drugs
- $\ensuremath{\mathfrak{S}}$ Poor have less access to medical services: if they want to abort, they may be sterile after a medical mistake + no access to IVF
- Poor live in more polluted areas: \(\sqrt{} \) fecundity

Important: c^{\min} is a technological constraint and not a preference parameter.

Budget constraints

Single men:

$$\bar{c}^m = w^m + a^m - \mu$$

 μ : cost of running a household

Single women:

$$c^{f} + \phi (1 + \eta(n)) w^{f} n = w^{f} + a^{f} - \mu$$

Couples:

$$c^{f} + c^{m} + \phi (1 + \eta(n)) \left(\alpha w^{f} + (1 - \alpha) w^{m} \right) n = w^{m} + w^{f} + a^{m} + a^{f} - \mu$$

 $\alpha \in (\frac{1}{2}, 1)$ mother's share of child support

with fixed cost of having children:

$$\eta(n) = \begin{cases} \frac{\eta}{n} & \text{if } n > 0 \\ 0 & \text{if } n = 0 \end{cases}$$

Maximum fertility

Single women:

$$0 \le n \le \frac{1 - \phi \eta}{\phi} \equiv \bar{n}_{\mathsf{M}}$$

Couples:

$$0 \le n \le \frac{1 - \alpha \phi \eta}{\alpha \phi} \equiv n_{\mathsf{M}}$$

Regimes

Several constraints may bind: maximum fertility, minimum consumption to procreate

Conditionally on being married or not, \exists thresholds for wages and non-labor income separating different regimes.

11 regimes total.

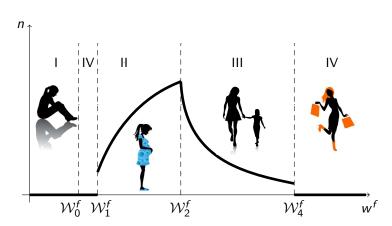
5 pictures.

Fertility conditionally on being single when $a^f \in [\underline{a}, \overline{a}[$

I: Involuntary childlessness II: "Get fit to procreate"

III: Interior solution

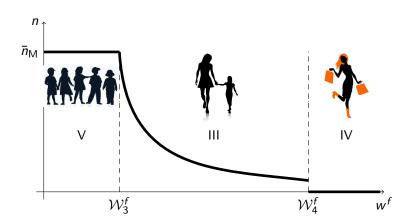
IV: Voluntary childlessness



Fertility conditionally on being single when $a^f \geq \overline{a}$

V: Maximum fertility

III: Interior solution
IV: Voluntary childlessness



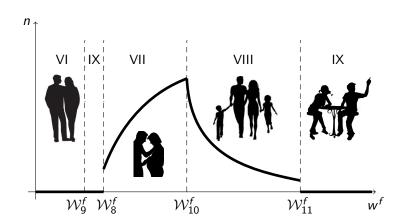
Fertility conditionally on being married when $a^t \in [A_0, A_1[$

VI: Involuntary childlessness

VII: "Eat and procreate"

IX: Voluntary childlessness

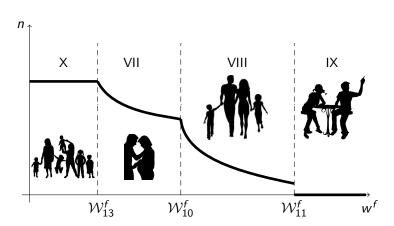
VIII: Interior solution



Fertility conditionally on being married when $a^f \in [A_1, A_2[$

X: "Eat and procreate" a maximum VII: "Eat and procreate"

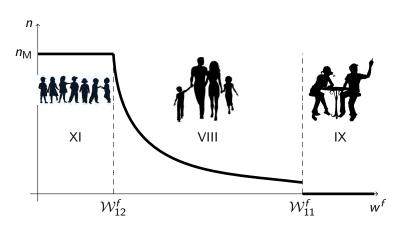
IX: Voluntary childlessness VIII: Interior solution



Fertility conditionally on being married when $a^f \geq A_2$

XI: Maximum fertility

VIII: Interior solution
IX: Voluntary childlessness



Identification of the Parameters

d, vector of 48 moments to match: fertility and childlessness rates for married and singles in 12 education categories

with p, vector of 9 parameters

We minimize

$$[d - s(p)][W][d - s(p)]'$$

where s(p) is the vector of simulated moments. W is the optimal weighting matrix.

To minimize the function, we implement in Fortran 90:

- **PIKAIA** (genetic algorithm from Charbonneau (2002)) \Rightarrow finds the region where the global maximum lies
- ② UOBYQA (quadratic approximation) ⇒ faster algorithm

How the simulated moments are computed

We consider a large number of hypothetical women, having a potential labor income depending on education

$$w_e = \gamma \exp\{0.1e\}, \quad \gamma = 0.9$$

For each woman we draw

- a non labor income from a log-normal distribution (mean and variance are parameters to be identified)
- a potential husband, with random education level and non-labor income

We compute whether each potential couple will marry, and what will be the optimal fertility of the woman

Simulated moments obtained by aggregating all individual choices

Identified parameters

Description	Parameter	Value	Std. Error
variance of the log normal distribution	σ_{a}	0.319	0.006
ratio of non labor income to labor income	m _a	0.868	0.011
preference parameter	ν	6.848	0.112
min consumption level to procreate	c ^{min}	0.339	0.004
good cost to be supported by a household	μ	0.333	0.005
bargaining parameter	$\underline{\theta}$	0.568	0.009
fraction of childrearing by women	α	0.596	0.005
time cost of having children	ϕ	0.216	0.007
fixed cost of children	η	0.225	0.002

Comments on parameters

 σ_a implies Gini on life-cycle income w^f+a^f equal to 0.17.

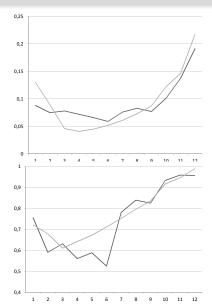
 $\underline{\theta}$ implies minimal negotiation power of a spouse $\underline{\theta}/2=0.28$

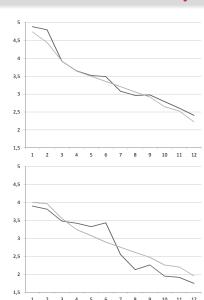
$$\eta$$
, ϕ , $\alpha \rightarrow n_{\rm M} = 7$, while $\bar{n}_{\rm M} = 4$.

 η means first child costs 22% more time than second

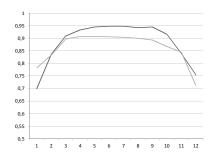
 $\alpha = 0.598$ fathers do a lot. (or ex ante expectations?)

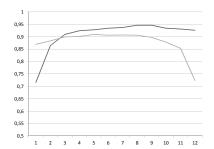
Matched moments: childlessness and mothers' fertility





Matched moments: marriage rates





NB: we did not not use marriage rates to identify the parameters

% of women in each regime by education category

	l	Ш	IV	V	VI	VII	VIII	IX	Χ	ΧI
	6	1	*	ikkhi	M	A	1	AN	A PARI	HHHH
1	15.7	0.0	0.0	6.1	10.2	43.5	7.1	0.0	4.2	13.2
2	11.3	0.2	0.0	5.2	7.4	40.9	20.0	0.0	0.9	14.1
3	6.2	1.3	0.1	2.8	3.1	17.7	58.3	1.0	0.0	9.5
4	5.7	1.6	0.3	1.7	0.9	4.2	76.1	2.8	0.0	6.7
5	5.7	1.7	0.6	1.3	0.4	0.9	80.3	3.7	0.0	5.4
6	5.7	1.8	1.0	1.0	0.1	0.1	81.6	4.6	0.0	4.3
7	5.6	1.7	1.6	0.7	0.0	0.0	81.6	5.5	0.0	3.3
8	5.5	1.5	2.5	0.5	0.0	0.0	81.0	6.5	0.0	2.4
9	5.1	1.4	3.8	0.4	0.0	0.0	79.8	7.7	0.0	1.8
10	2.5	0.9	9.7	0.2	0.0	0.0	75.3	10.6	0.0	8.0
11	1.0	0.7	13.7	0.1	0.0	0.0	71.7	12.3	0.0	0.5
12	0.0	0.3	28.4	0.0	0.0	0.0	55.7	15.5	0.0	0.1
all	5.3	1.5	3.1	0.9	0.5	2.5	76.7	5.9	0.1	3.6

Involuntary childlessness

	-	III	IV	V	VI	VII	VIII	IX	Х	ΧI
	6				M					
1	15.7	0.0	0.0	6.1	10.2	43.5	7.1	0.0	4.2	13.2
2	11.3	0.2	0.0	5.2	7.4	40.9	20.0	0.0	0.9	14.1
3	6.2	1.3	0.1	2.8	3.1	17.7	58.3	1.0	0.0	9.5
4	5.7	1.6	0.3	1.7	0.9	4.2	76.1	2.8	0.0	6.7
5	5.7	1.7	0.6	1.3	0.4	0.9	80.3	3.7	0.0	5.4
6	5.7	1.8	1.0	1.0	0.1	0.1	81.6	4.6	0.0	4.3
7	5.6	1.7	1.6	0.7	0.0	0.0	81.6	5.5	0.0	3.3
8	5.5	1.5	2.5	0.5	0.0	0.0	81.0	6.5	0.0	2.4
9	5.1	1.4	3.8	0.4	0.0	0.0	79.8	7.7	0.0	1.8
10	2.5	0.9	9.7	0.2	0.0	0.0	75.3	10.6	0.0	8.0
11	1.0	0.7	13.7	0.1	0.0	0.0	71.7	12.3	0.0	0.5
12	0.0	0.3	28.4	0.0	0.0	0.0	55.7	15.5	0.0	0.1
all	5.3	1.5	3.1	0.9	0.5	2.5	76.7	5.9	0.1	3.6

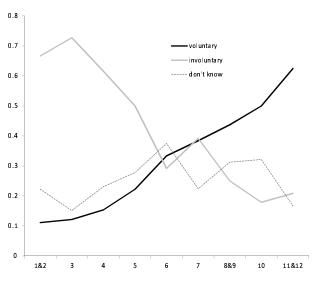
Marriage helps to escape poverty

		Ш	IV	V	VI	VII	VIII	IX	Χ	XI
						A			a de de	
1	15.7	0.0	0.0	6.1	10.2	43.5	7.1	0.0	4.2	13.2
2	11.3	0.2	0.0	5.2	7.4	40.9	20.0	0.0	0.9	14.1
3	6.2	1.3	0.1	2.8	3.1	17.7	58.3	1.0	0.0	9.5
4	5.7	1.6	0.3	1.7	0.9	4.2	76.1	2.8	0.0	6.7
5	5.7	1.7	0.6	1.3	0.4	0.9	80.3	3.7	0.0	5.4
6	5.7	1.8	1.0	1.0	0.1	0.1	81.6	4.6	0.0	4.3
7	5.6	1.7	1.6	0.7	0.0	0.0	81.6	5.5	0.0	3.3
8	5.5	1.5	2.5	0.5	0.0	0.0	81.0	6.5	0.0	2.4
9	5.1	1.4	3.8	0.4	0.0	0.0	79.8	7.7	0.0	1.8
10	2.5	0.9	9.7	0.2	0.0	0.0	75.3	10.6	0.0	8.0
11	1.0	0.7	13.7	0.1	0.0	0.0	71.7	12.3	0.0	0.5
12	0.0	0.3	28.4	0.0	0.0	0.0	55.7	15.5	0.0	0.1
all	5.3	1.5	3.1	0.9	0.5	2.5	76.7	5.9	0.1	3.6

Voluntary childlessness

							\ // III	13.7		271
	I	Ш	IV	V	VI	VII	VIII	IX	Χ	ΧI
			*					M		
1	15.7	0.0	0.0	6.1	10.2	43.5	7.1	0.0	4.2	13.2
2	11.3	0.2	0.0	5.2	7.4	40.9	20.0	0.0	0.9	14.1
3	6.2	1.3	0.1	2.8	3.1	17.7	58.3	1.0	0.0	9.5
4	5.7	1.6	0.3	1.7	0.9	4.2	76.1	2.8	0.0	6.7
5	5.7	1.7	0.6	1.3	0.4	0.9	80.3	3.7	0.0	5.4
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8	5.5	1.5	2.5	0.5	0.0	0.0	81.0	6.5	0.0	2.4
9	5.1	1.4	3.8	0.4	0.0	0.0	79.8	7.7	0.0	1.8
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11	1.0	0.7	13.7	0.1	0.0	0.0	71.7	12.3	0.0	0.5
12	0.0	0.3	28.4	0.0	0.0	0.0	55.7	15.5	0.0	0.1
all	5.3	1.5	3.1	0.9	0.5	2.5	76.7	5.9	0.1	3.6

NSFG data: 1973 & 1976



Very detailed survey on fertility, but few observations

Historical experiment

1960-1990: rise in the education of both women and men

Predictions of the model are:

- A. drop in marriage rates for unskilled women, rise for skilled.
- B. a drop in childlessness for all education categories.
- C. drop in fertility (opportunity cost effect dominates).

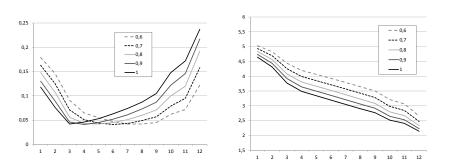
A and B are in the data. C is not because of baby boom.

Imposing $\alpha=1$, the model becomes unable to reproduce

- (a) a reasonable marriage rate (especially for highly educated women who have lost their incentive to marry),
- (b) the U-shaped relationship between education and childlessness for married women,
- (c) the gap between fertility of the married mothers and fertility of the single mothers, who now face the same opportunity cost.

Hence, allowing $\alpha < 1$ is pretty important.

Closing the gender wage gap γ



Usual opportunity cost effect on fertility.

Drop in Involuntary Childlessness and rise in Voluntary Childlessness

Conclusion (1)

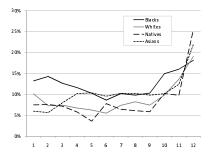
Distinguish the decision to have children or not from the choice of the number of children \Rightarrow highlighting, both in terms of data and theory.

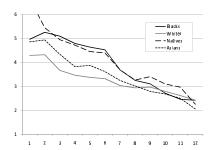
- 3 stylized facts \Rightarrow the model is relevant to explain them
- New "regimes" of fertility which are relevant in the data:
 - 5.8% of American women are involuntarily childless in 1990
 - 9% are voluntarily childless
- Co-existence of voluntary and involuntary childlessness explains U-shaped relationship between childlessness and education (for both married and single women)

Conclusion (2)

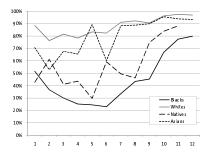
- Marriage interacts in two ways with childlessness:
 - for poor woman \Rightarrow an opportunity to get enough resources to be able to have children \Rightarrow reduces involuntary childlessness.
 - for rich women, marriage reduces the opportunity cost of having children \Rightarrow reduces voluntary childlessness.
- The model helps to understand the impact of education on marriage, fertility and childlessness between 1960 and 1990

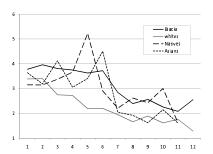
Childlessness and fertility of mothers (married)



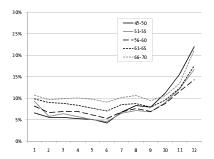


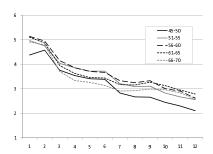
Childlessness and fertility of mothers (single)



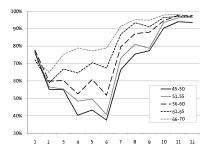


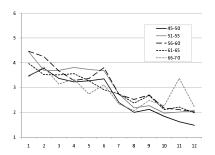
Childlessness and fertility of mothers (married)





Childlessness and fertility of mothers (single)





Percentage of single mothers, aged 45-70, with an unmarried partner

Cat.	%	Cat.	%
1	3.8	7	3.6
2	4.8	8	2.8
3	4.0	9	3.8
4	3.6	10	3.0
5	3.8	11	2.8
6	4.0	12	8.2